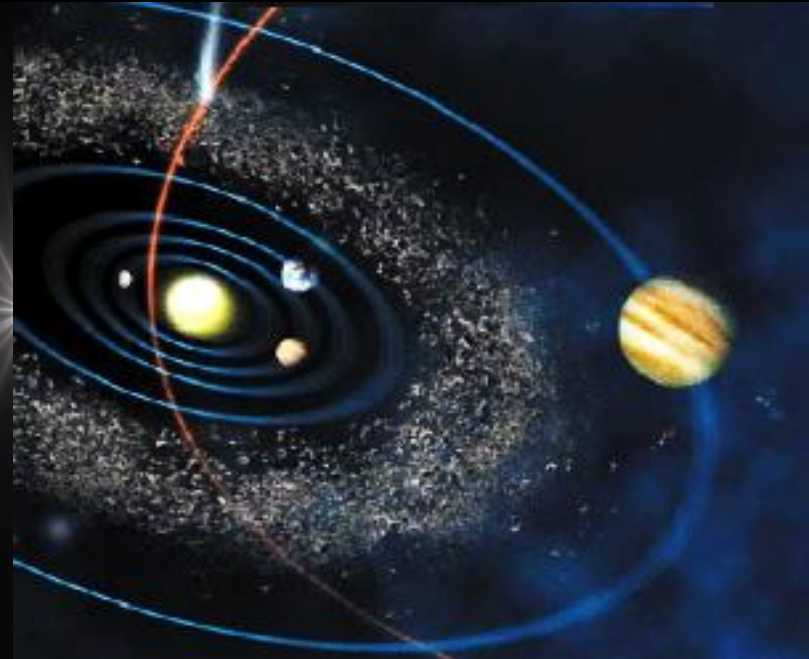
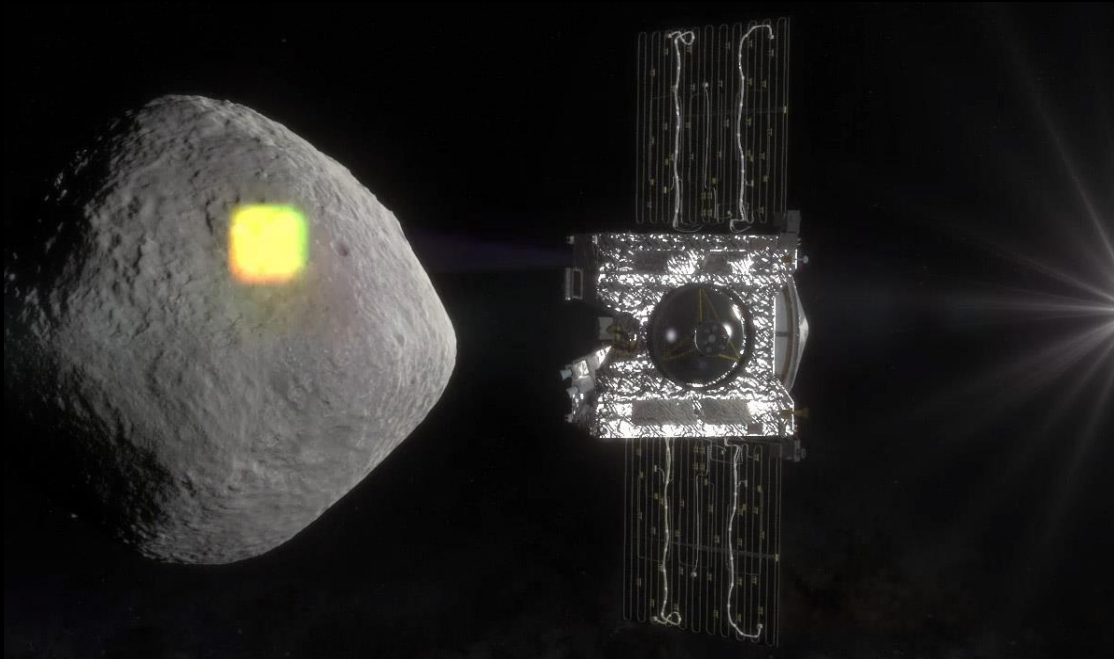


**SpaceTrex**



# Trajectory design for asteroid surface mapping missions with flybys of spacecraft swarms

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# Outline

- Motivation
- Objective
- Challenges
- Approach
- Simulation
- Results
- Discussion
- Future work



## Motivation



Geo-history



Security/Deflection



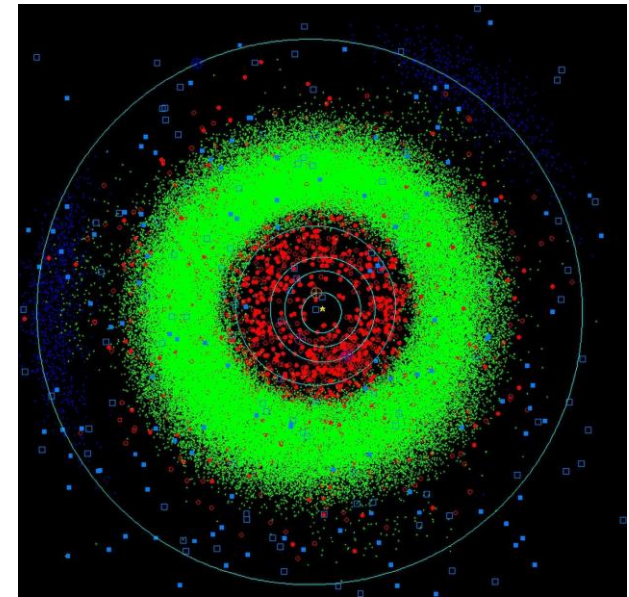
ISRU

**Asteroid exploration is tied to planetary science,  
security, space economy.**



## Motivation

- 2 million asteroids estimated in the main asteroid belt.
- 17,000 asteroids found near earth.
- They hold valuable resources such as water, carbon and rare metals that may one day support a spacefaring civilization.



Main belt and near-Earth  
Asteroids

**Asteroids can be pitstops for interplanetary travel**





## Motivation

- Surface maps yield crucial geological information of the asteroid:
  - Orbit
  - Composition
  - Density
  - Shape
  - Gravity field



Asteroid Bennu

**Surface mapping missions pave the way for surface exploration missions**



## The Swarm approach

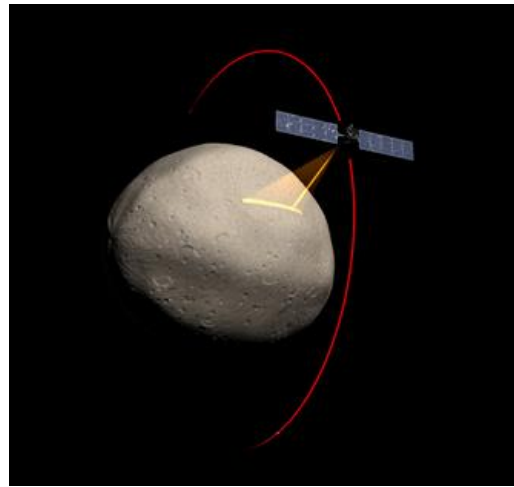
- *“Whole greater than the sum of the parts”*
- Solve a complex task using many individuals.
- Individuals are simple, low-cost, disposable.



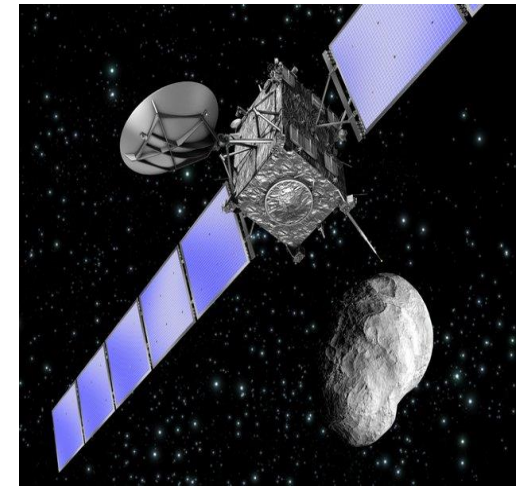


## Mapping trajectories

- The mapping trajectories of the spacecraft, can be broadly classified into 2 types, when surface interactions are not considered:
  - Orbits
  - Flybys



DAWN's orbit around Vesta



Rosetta's flyby of Steins



# Trajectory comparison

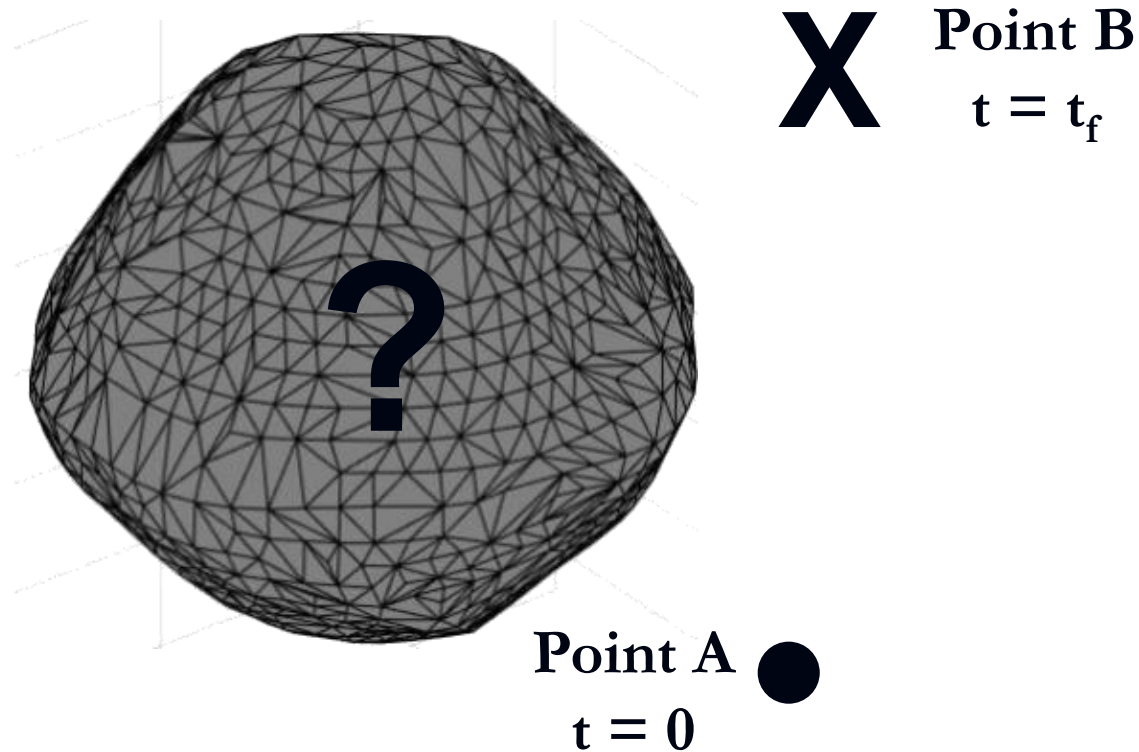
Flyby	Orbits
<p><b>Pros:</b></p> <ul style="list-style-type: none"><li>• Ideal for short period observations</li><li>• Relatively fuel efficient</li><li>• Single spacecraft design can be used for multiple targets</li><li>• Can be extended to observe multiple targets</li><li>• Swarm deployment is easier compared to orbital operations</li></ul> <p><b>Cons:</b></p> <ul style="list-style-type: none"><li>• Sun vector is a crucial factor for visual observations</li><li>• Shorter inspection times</li><li>• Multiple flybys may be required to completely observe the target</li></ul>	<p><b>Pros:</b></p> <ul style="list-style-type: none"><li>• Dedicated to single target body observations</li><li>• Suitable for long term observations</li><li>• Sun vector is not a crucial factor</li></ul> <p><b>Cons:</b></p> <ul style="list-style-type: none"><li>• Orbit insertion burns are fuel expensive</li><li>• Susceptible to gravitational instabilities</li><li>• Spacecrafts need to be separately designed for different target bodies</li><li>• Difficult to deploy an orbiting constellation</li></ul>

**Flybys are suitable for low cost, low thrust missions; can be deployed on a spacecraft swarm**





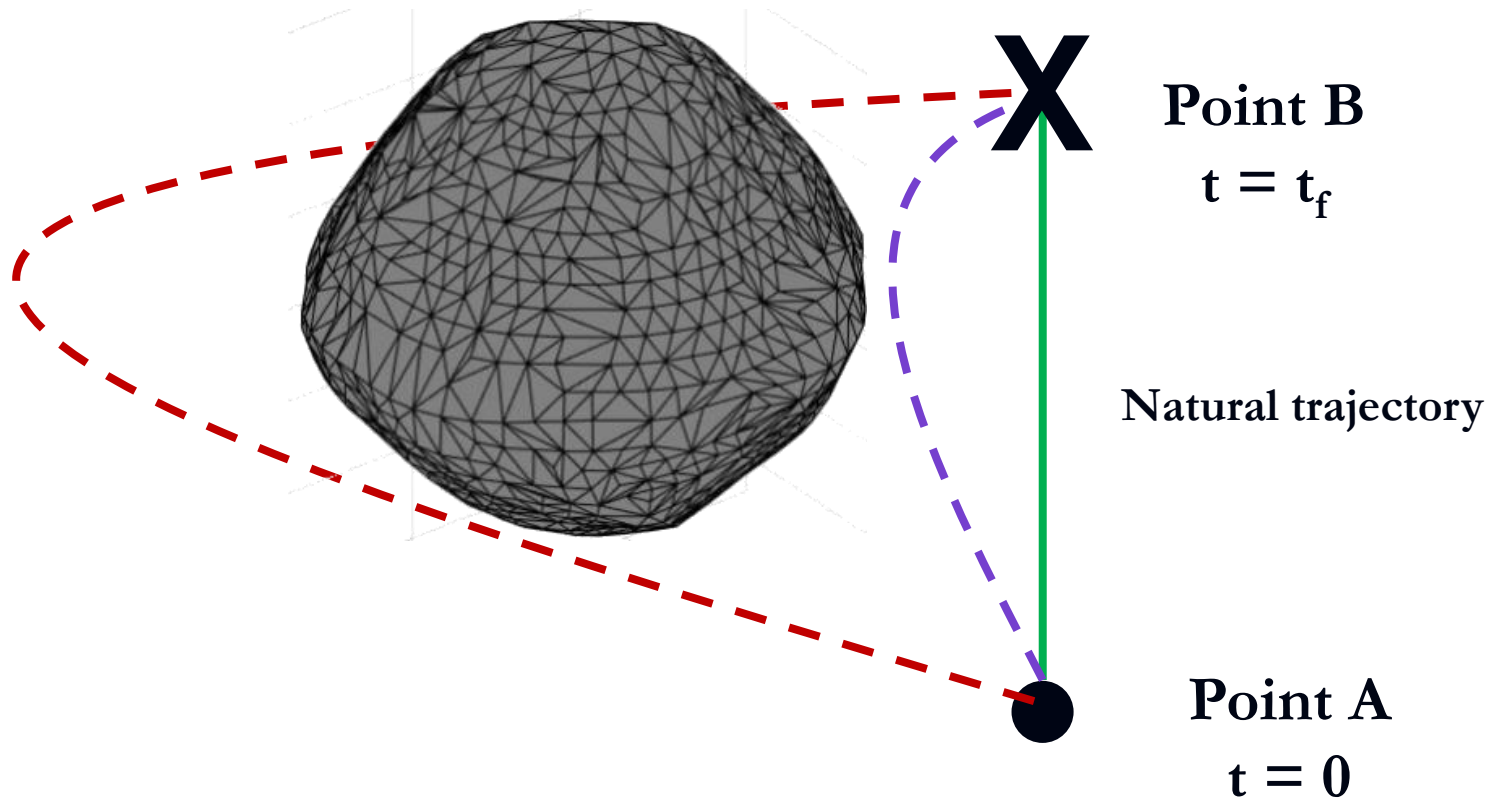
# Trajectory design



Objective is to find a trajectory that connects the current position to its destination in desired time



# Trajectory design



Trajectories allowed by the dynamics minimize fuel



## Objective

- To find the trajectories allowed by local gravity field, which takes a spacecraft from its current location to a desired location within a given time.
- Extend this to find trajectories for spacecraft swarm, so that all spacecrafts reach their destinations within specified times.



## Challenges

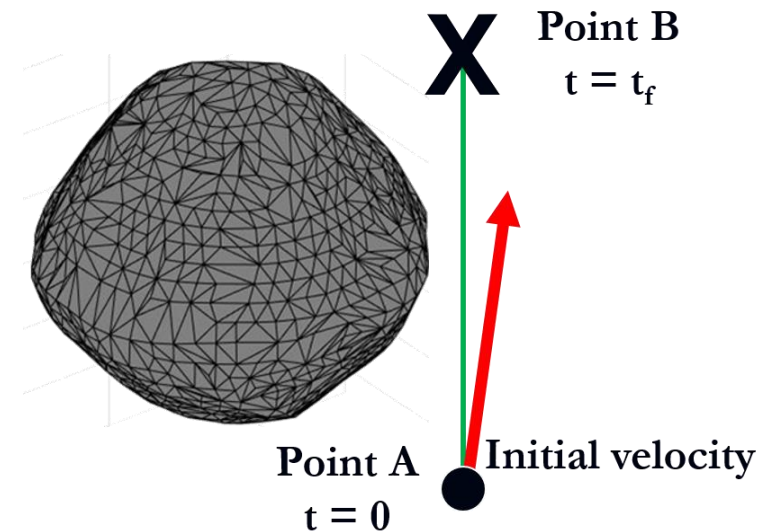
- **Complex dynamics around around the asteroid.**
- **Each asteroid exhibits different dynamics.**
- **Solar radiation is a significant perturbation**
- **Keplerian tools cannot be used to design trajectories.**





## Problem reduction

- For a given initial and final positions, and a flyby time, the trajectory is specified by finding the required initial velocity.



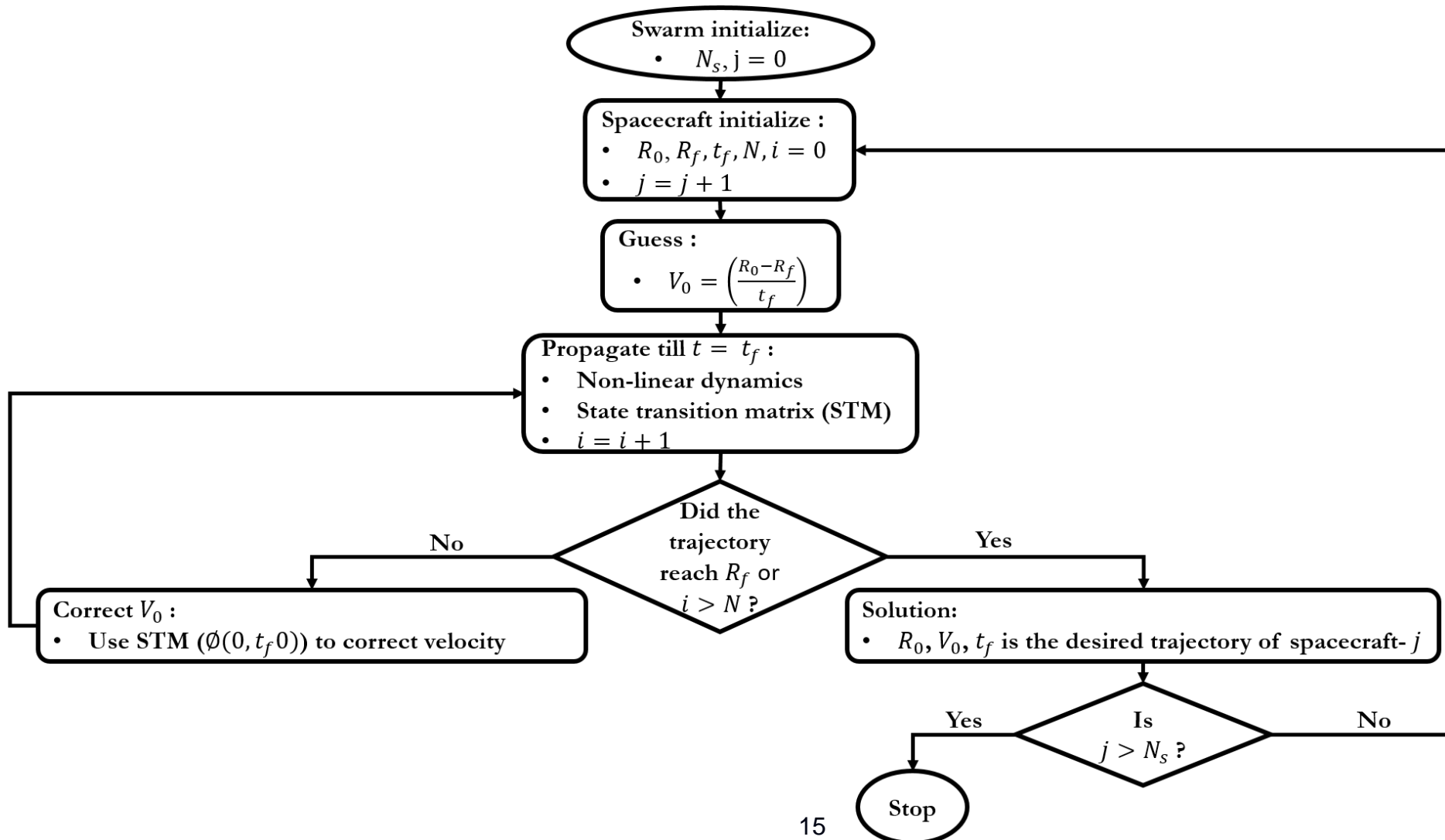


## Approach

- Iterative schemes to search for the desired initial condition are developed.
- The schemes are performed over the entire swarm population to obtain required initial conditions
- The initial conditions are then propagated forward in time to obtain the trajectories
- Gravity, solar tide, and SRP are used to model the dynamics



# Trajectory design algorithm





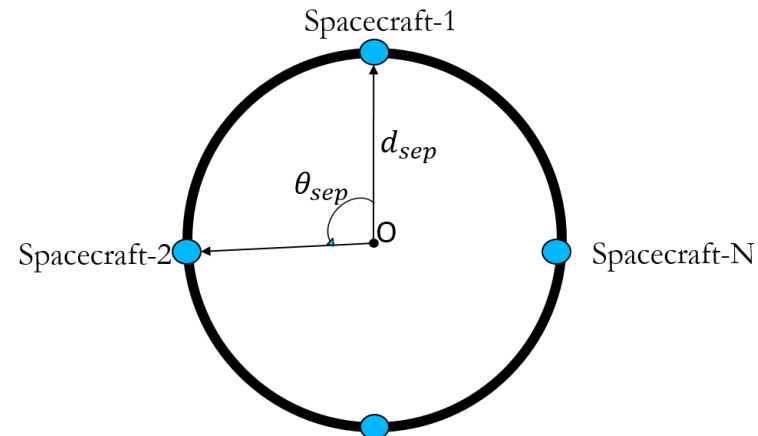
## Spacecraft swarm

- A ring shaped spacecraft swarm of  $N$  uniformly separated spacecraft as follows
- The location of the  $j^{\text{th}}$  spacecraft is given by:

$$R_j = \begin{bmatrix} d_{sep} \cos(j-1)\theta_{sep} \\ d_{sep} \sin(j-1)\theta_{sep} \\ z \end{bmatrix}$$

- Where:

$$\theta_{sep} = \frac{2\pi}{N}$$



Swarm layout





## Simulations

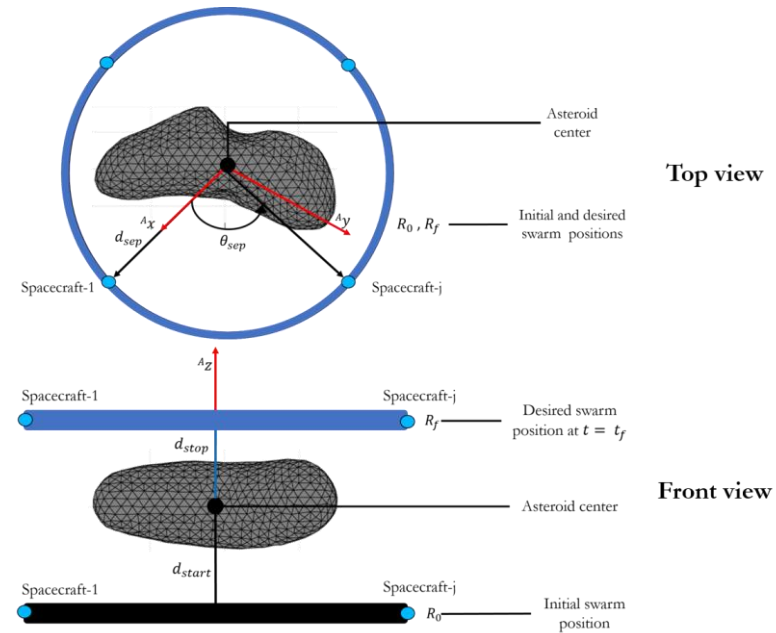
- The trajectory design algorithm is demonstrated for the ring shaped swarm.
- The Swarm is desired to fly by the asteroid 433 Eros
- The spacecrafts need to maintain a radial separation of 50 Km from the center of the asteroid
- The spacecrafts are desired to travel a distance of 60 km along the spin axis of the asteroid in 10 minutes
- Nominal 12U CubeSat parameters are used for the spacecraft model



# Swarm simulations

- The following parameters were used for simulating the flyby with the spacecraft swarm

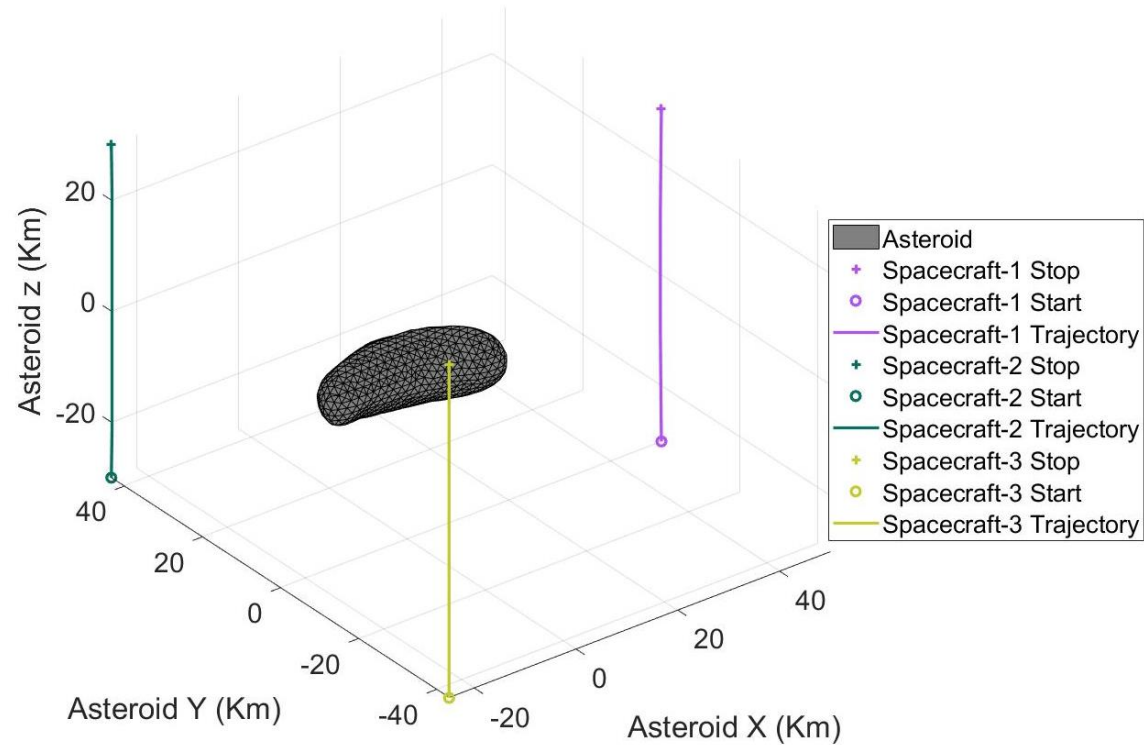
Parameter	Value
Asteroid	433 Eros
Number of spacecraft	3, 4, 5
Radial separation (Km)	50
Starting distance (Km)	-30
Stopping distance (Km)	30
Flyby duration (mins)	10



Targeting geometry with the spacecraft swarm



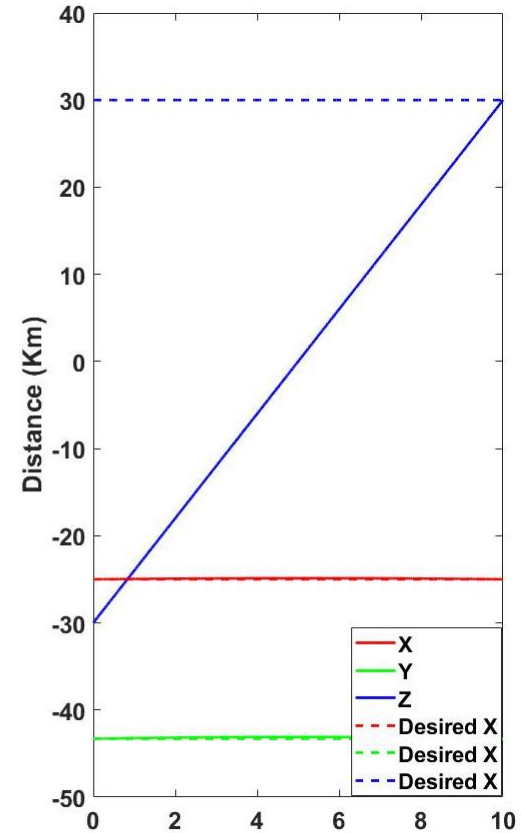
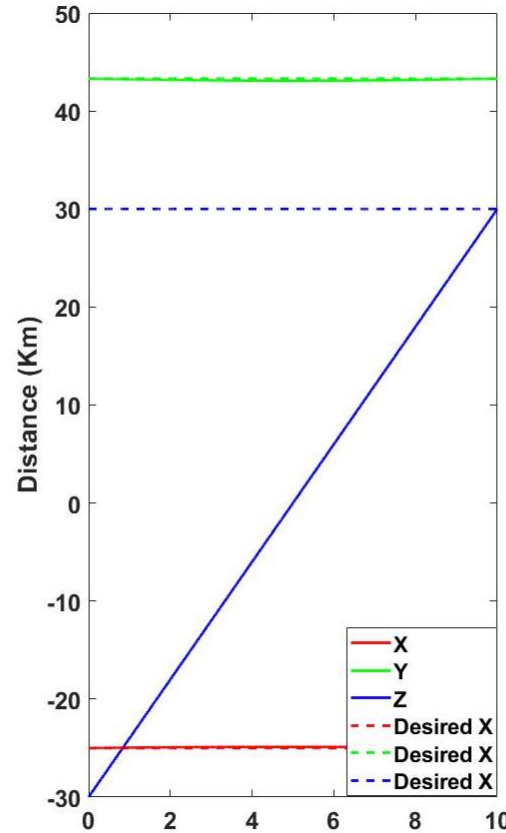
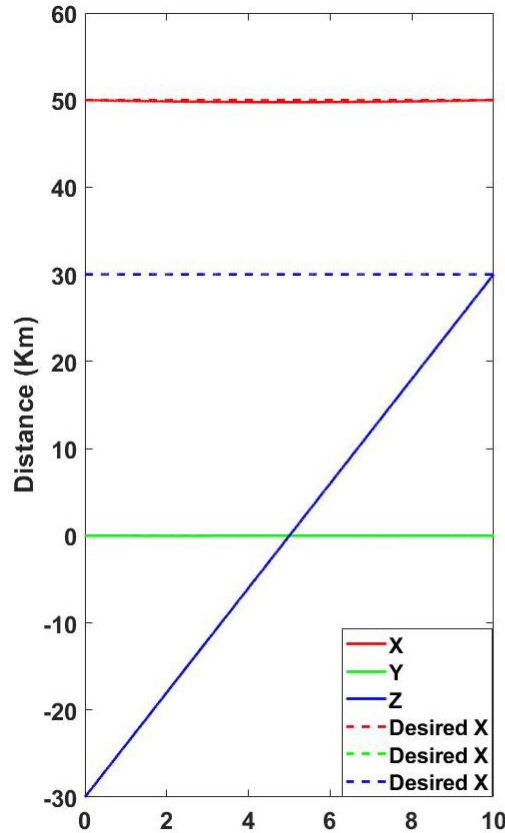
# 3 spacecraft trajectories



The trajectories generated for 3 spacecrafts



# Spacecraft positions

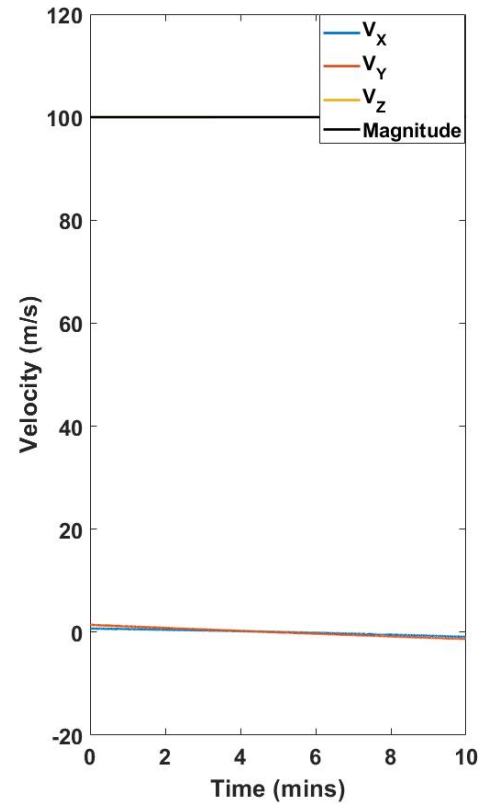
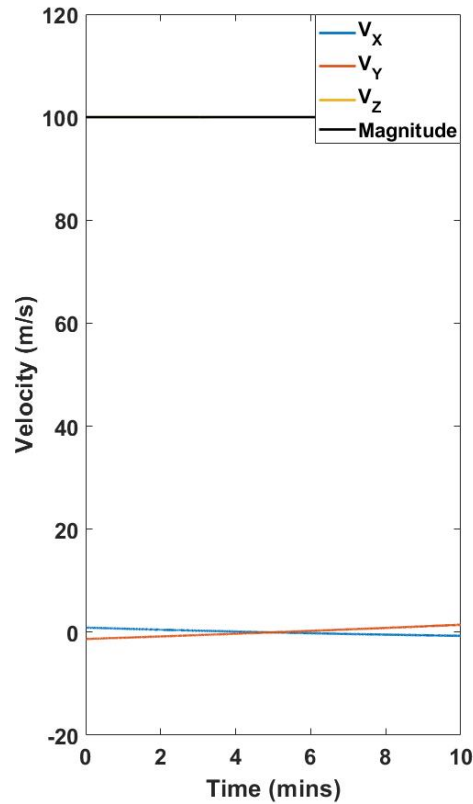
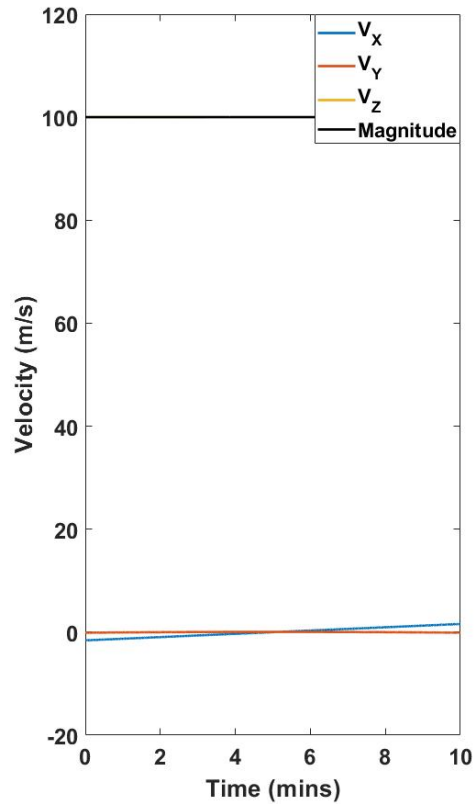


The algorithm yields desired flyby trajectories, with  
in the desired 10 minutes time





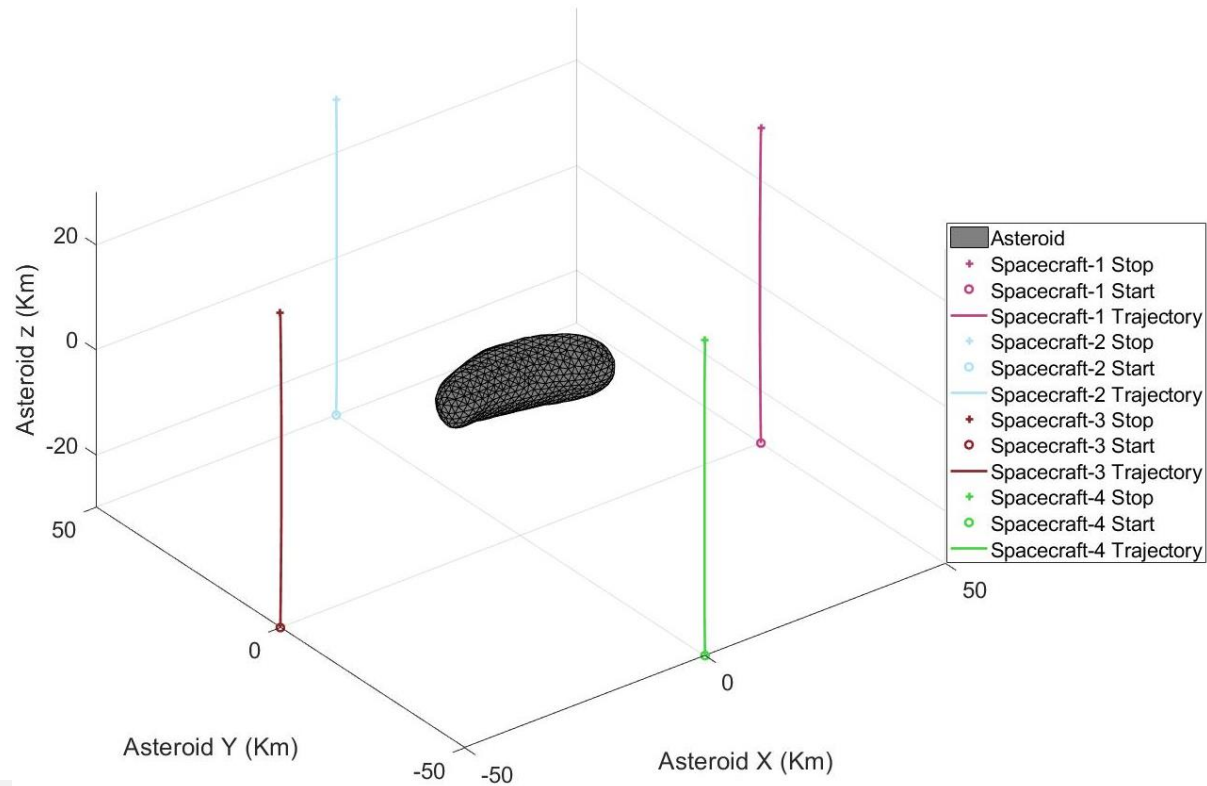
### 3 spacecraft flyby



All the spacecrafts fly with a 100 m/s velocity during the flyby



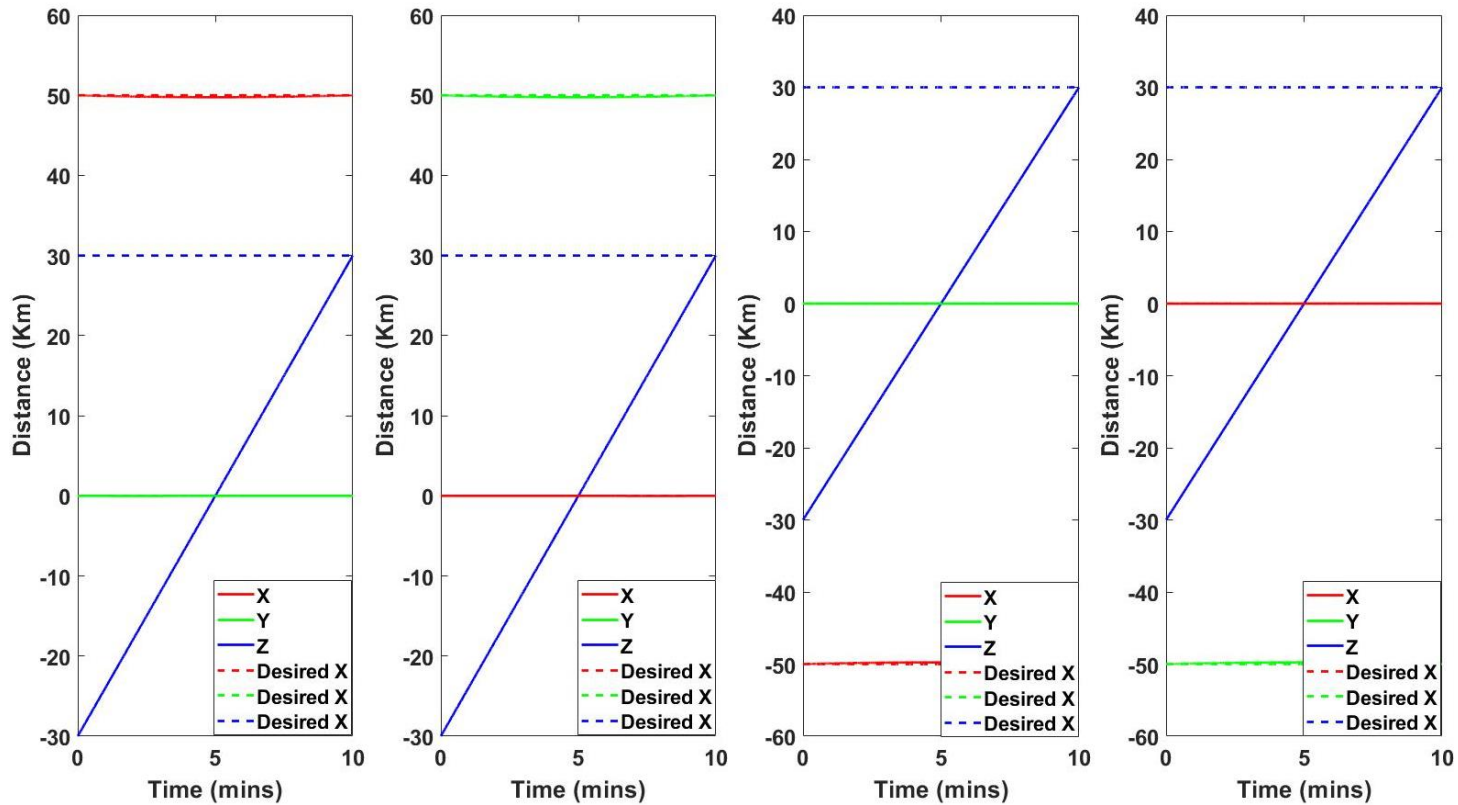
# 4 Spacecraft trajectories



The trajectories generated for 4 spacecraft



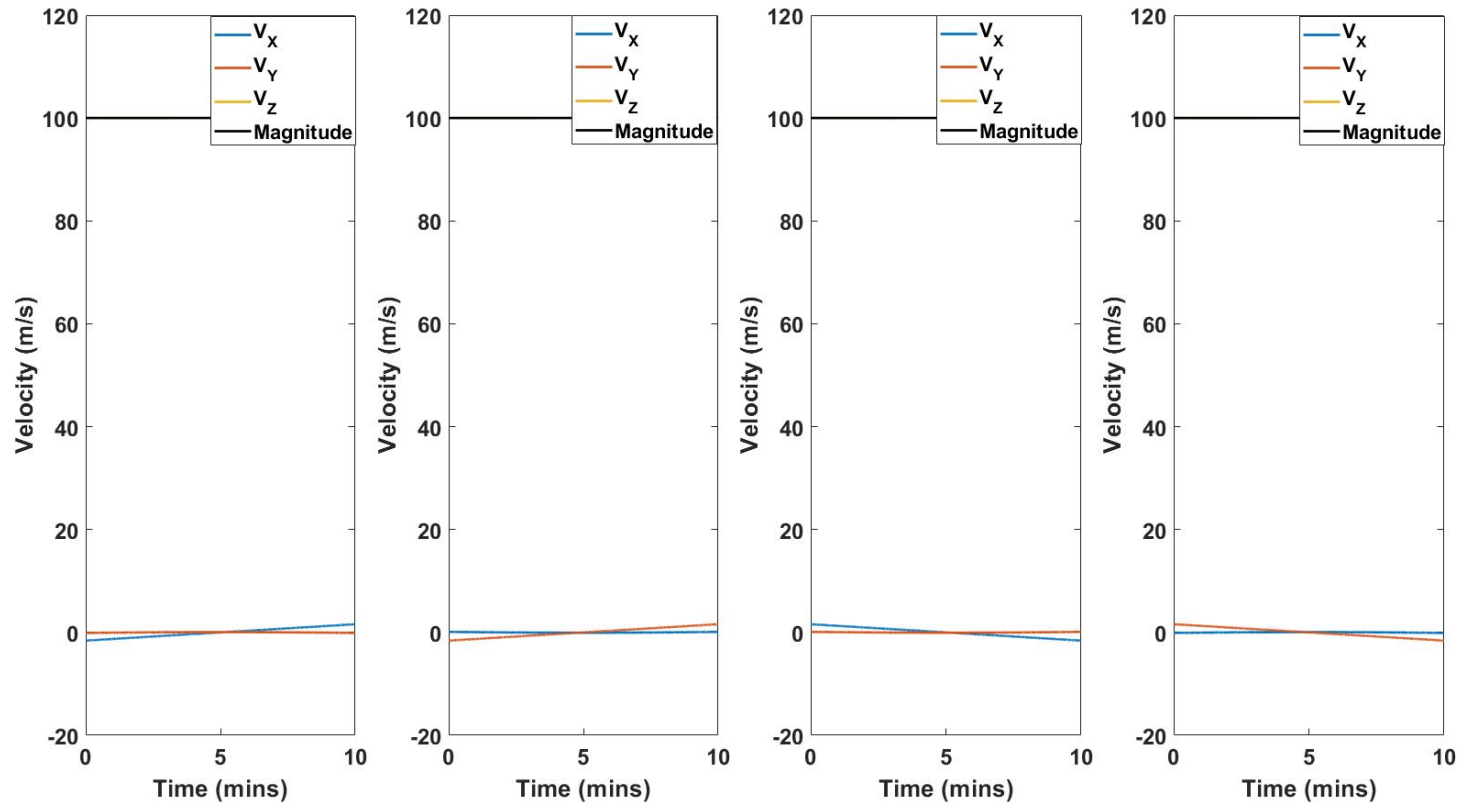
# Spacecraft positions



The algorithm yields desired flyby trajectories, with in the desired 10 minutes time



# Flyby velocities

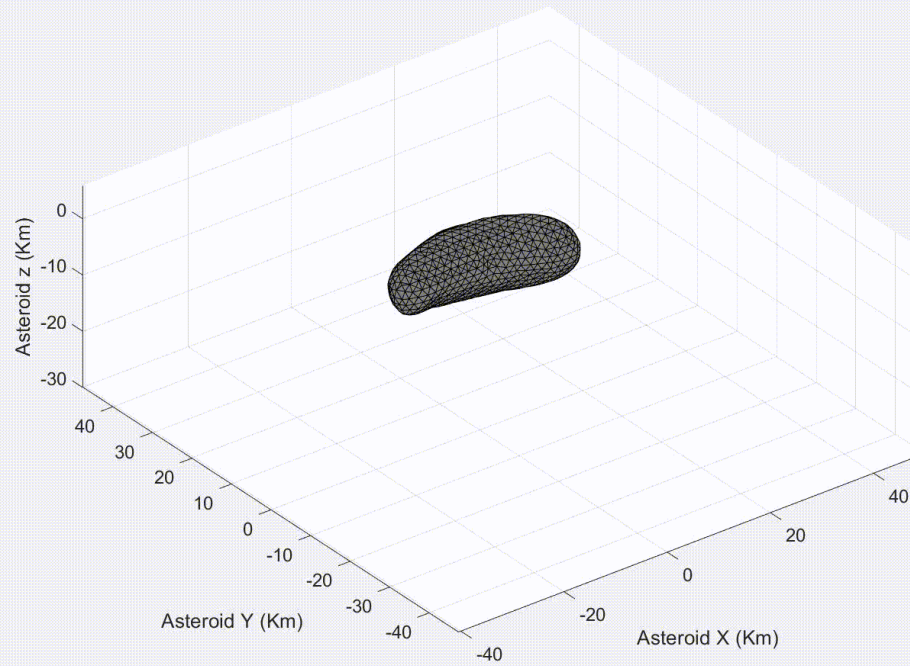


All the spacecrafts fly with a 100 m/s velocity during the flyby





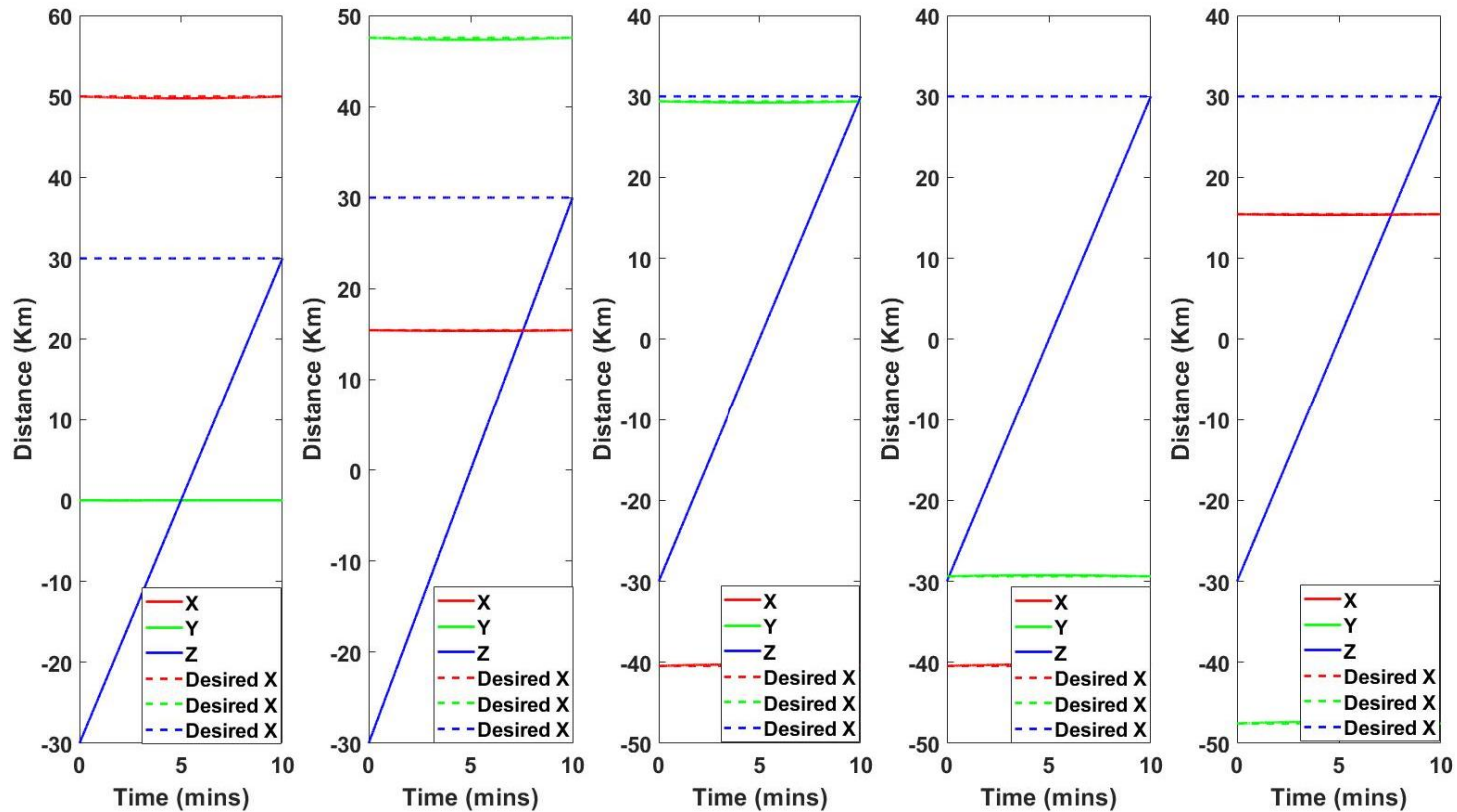
# Results



**The trajectories generated for 5 spacecrafts**



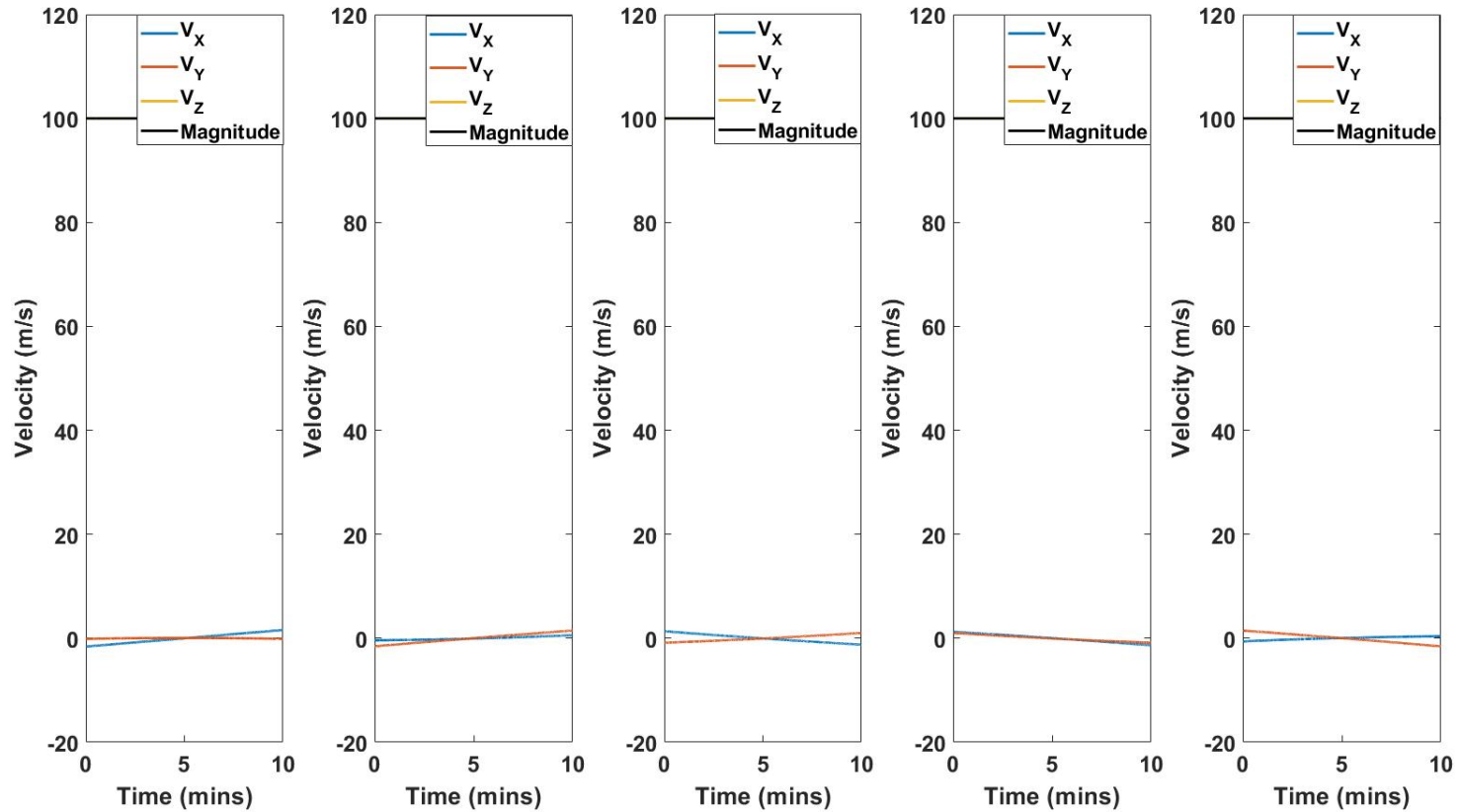
# Spacecraft positions



The algorithm yields desired flyby trajectories, with in the desired 10 minutes time



# Flyby velocities

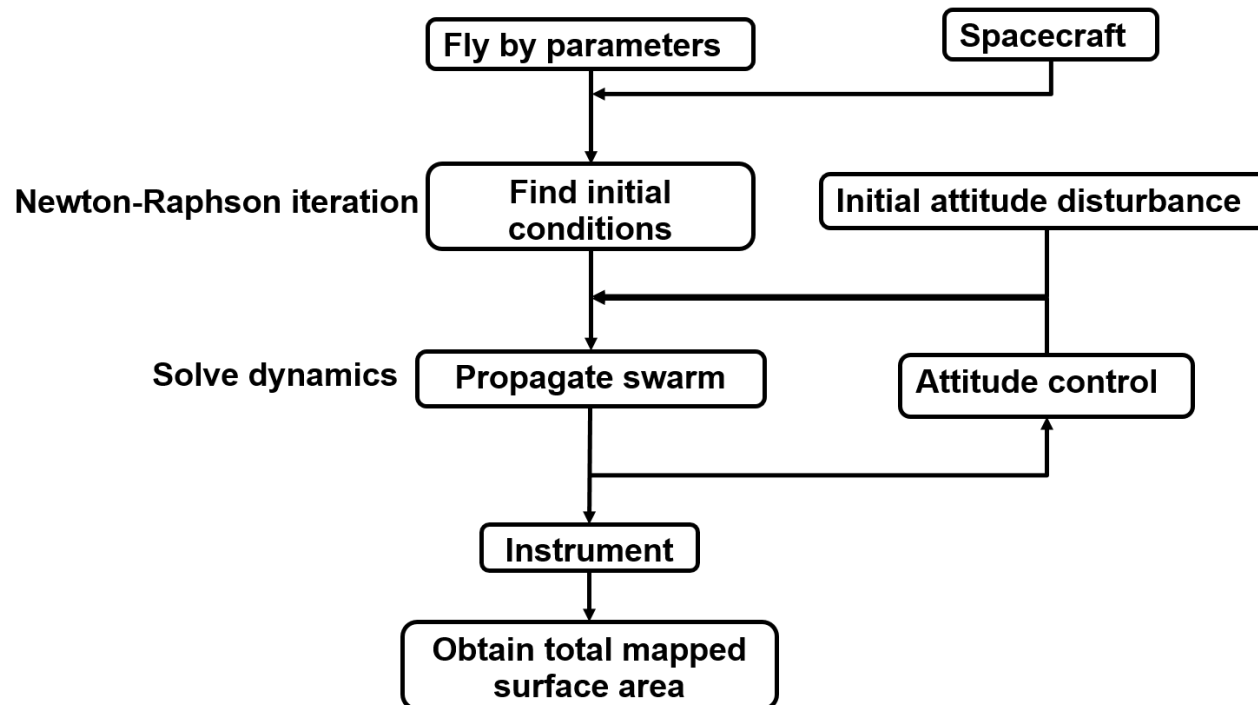


All the spacecrafts fly with a 100 m/s velocity during the flyby



# Mapping demonstration

- A mapping simulator which couples the trajectory and attitude control with the following architecture





## Results

- The simulator is demonstrated with 2 sets of attitude control strategies:
  - i. Nadir pointing
  - ii. Field of view Sweeping

**In both the cases, the area mapped by the instrument is noted**





## Instrument parameters

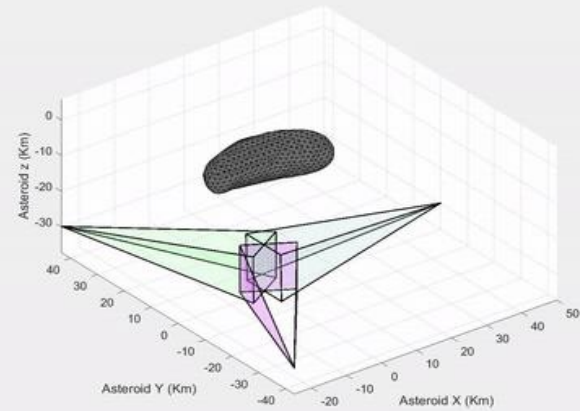
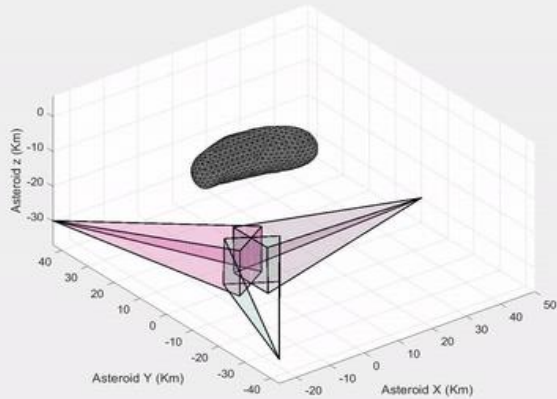
- The following are the parameters of the onboard instrument on the

Parameter	Value
FOV	15
Near distance (m)	0.1
Far distance (Km)	500,000
Frame rate (fps)	5

**A pinhole camera model is used to simulate the instrument**



# 3 Spacecraft mapping



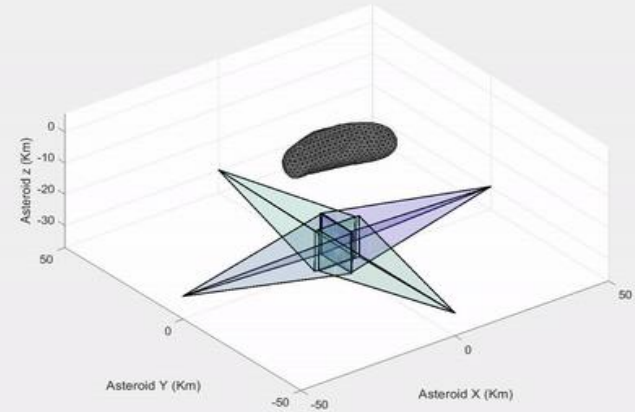
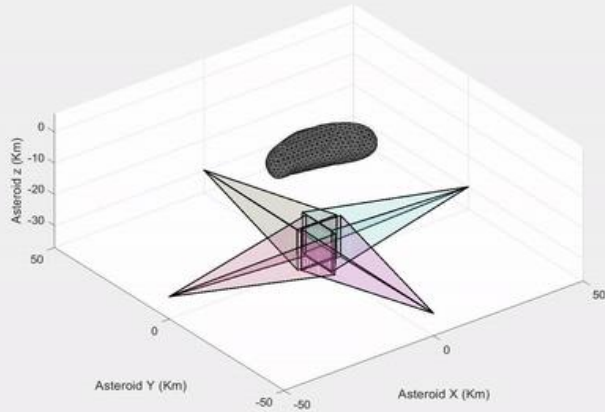
Nadir pointing

FOV Sweeping

Observed Area (Km <sup>2</sup> )	698.01	Observed Area (Km <sup>2</sup> )	1103.34
% Observed Area	63.26	% Observed Area	100



# 4 Spacecraft mapping



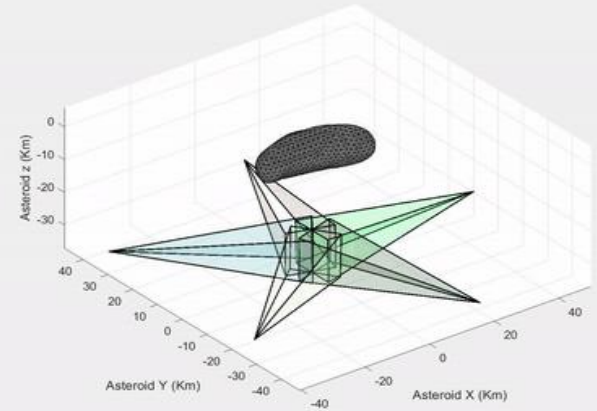
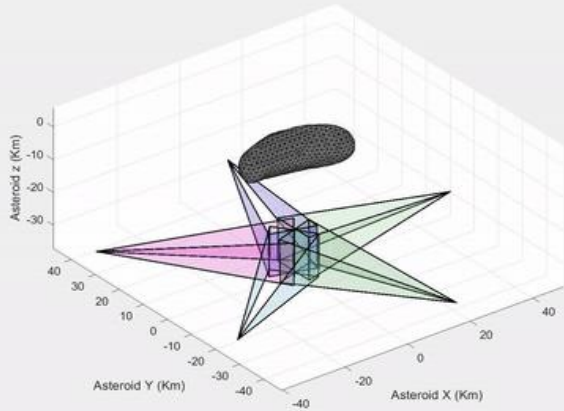
Nadir pointing

FOV Sweeping

Observed Area (Km <sup>2</sup> )	965.89	Observed Area (Km <sup>2</sup> )	1103.34
% Observed Area	87.54	% Observed Area	100



# 5 Spacecraft mapping



Nadir pointing

FOV Sweeping

Observed Area (Km <sup>2</sup> )	852.30	Observed Area (Km <sup>2</sup> )	1103.34
% Observed Area	76.24	% Observed Area	100



## Discussion

- **Surface mapping missions of asteroids yield rich geological information.**
- **Flyby trajectories performed by spacecraft swarm are better suited for surface mapping than orbits**
- **This work presented a trajectory design algorithm for a swarm of spacecrafts around asteroids**
- **The algorithm uses an iterative numerical scheme using the state transition matrix, to find the desired natural trajectories**





## Discussion

- The algorithm is demonstrated for a circularly symmetric swarm consisting of 3, 4, & 5 spacecrafts.
- The demonstrations showed a flyby around the asteroid 433 Eros, where the spacecrafts are required to travel at a speed of 100 m/s.
- These trajectories are then coupled with attitude control strategies to 100% surface mapping coverage.



## Future work

- Integrate with strategies to search for optimal mapping locations.
- Integrate with optimal attitude tracking strategies to improve coverage with minimal energy.
- Design flyby sequences to map multiple asteroids.

Thank You

Questions ?



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