

On the Formations of a CubeSat Constellation at the Earth-Moon L1 Libration Point Kevin Gomez¹, Charles H. Lee^{1,2}, Alessandra Babuscia², and Kar-Ming Cheung² ¹Department of Mathematics, California State University Fullerton CALIFORNIA STATE UNIVERSITY **FULLERTON**

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Goals of the study

•Examine various characteristics of halo orbits around the L1 point.

•Simulate the placement of 20 6U CubeSats in orbit around the L1 libration point of the Earth-Moon system.

•Develop station keeping strategy to maintain constellation with as little energy as possible and relative distances of 10km ~100km.

Introduction

SOLARA/SARA's Mission Concepts:

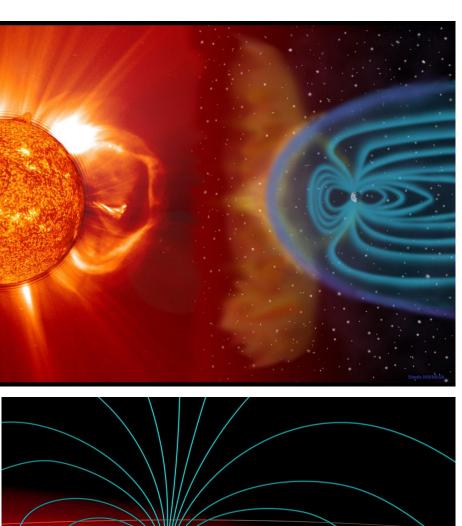
•Observe temporal and spatial evolution of solar weather and its interaction with Earth's magnetosphere.

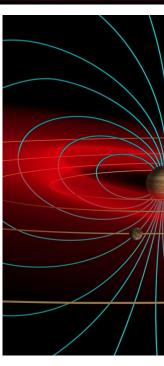
•Produce all-sky map in three bands between 30MHz and 30kHz with spatial resolution of at least 1 arcminute.

•Observe magnetospheric radio emissions from Jupiter, Saturn, Uranus, and Neptune with resolution of 10 arcseconds and search for planetary radio emission at the locations of known giant exoplanets.

•Test the feasibility of a MIMO system in the space environment.

•Demonstrate a communication data rate of at least one order of magnitude higher than traditional (low gain) CubeSat communication systems.





Model: CR3BP Earth-Moon System

For our study of Halo orbits we consider the non-dimensionalized CR3BP (Circular Restricted 3 Body Problem). The basic assumptions are:

• Moon follows circular orbit

•Mass of third body (i.e. satellite) has negligible gravitational effect.

•Gravitational force between two masses is given by,

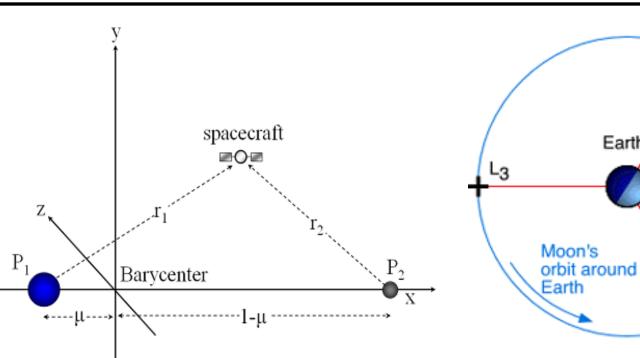
$$\vec{F} = \frac{Gm_1m_2}{r^3}\vec{r}$$

Earth-Moon System Libration Points

•Five Libration points exist.

•L1 is of primary interest due to its position do to benefits.

Earth and Moon are kept stationary on x-axis using a rotating frame, where (x,y) denotes satellite's position.	$x = X \cdot \cos(\frac{2\pi}{T})$ $y = X \cdot \sin(\frac{2\pi}{T})$
The normalized equations of motion are in the rotated frame are provided by,	$\ddot{x} - 2\dot{y} = -b$ $\ddot{y} + 2\dot{x} = -b$ $\ddot{z} = -b$
Linearization of the CR3BP problem is achieved with,	$\dot{\Phi}(t,t_0) = f'$ where, $ec{x}(t)$
Numerical solution for the trajectory and STM is computed by solving the first order system of ODEs to the right.	$\dot{\vec{x}}(t) = f(t)$



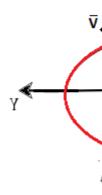
Numerical Procedures: Construction of Halo Orbits

The numerical solution for the STM allows for Differential Corrections that can approximate initial conditions leading to a halo orbit.

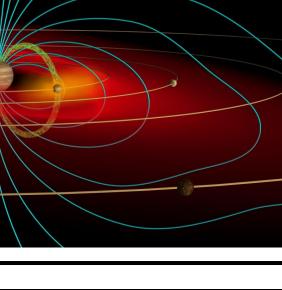
A periodic solution must satisfy at the start and midpoint of the orbit,

p_y	_	0
v_x	=	0
v_{z}	=	0

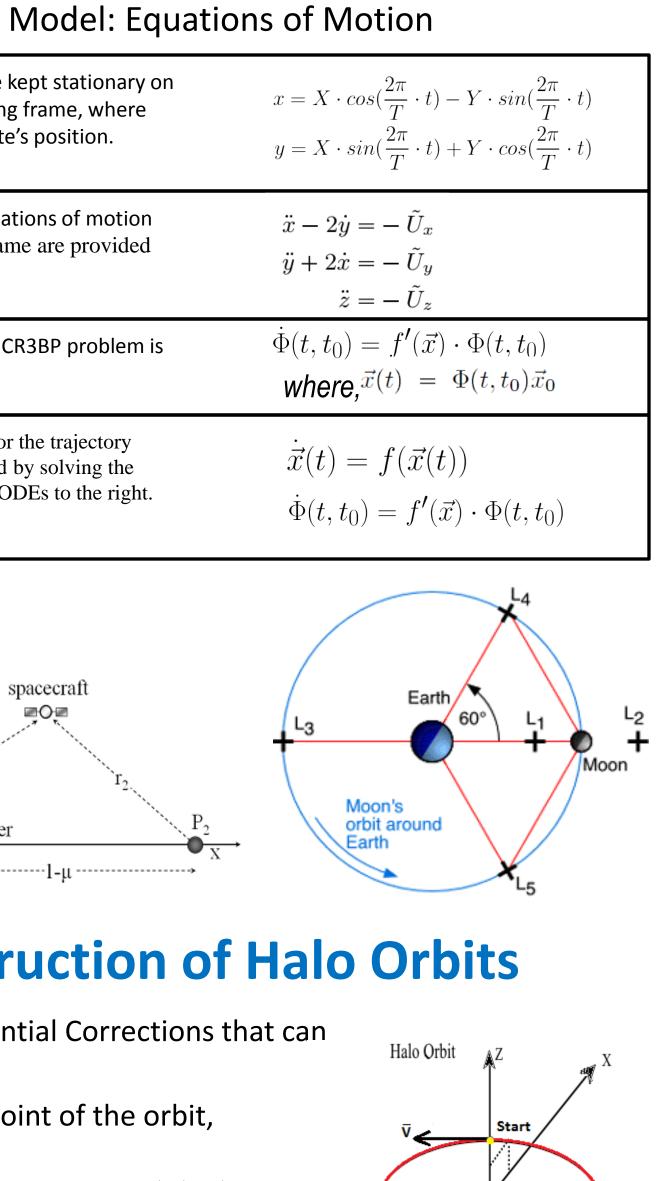
The first is the y position component, and the latter two are the x and z velocity components. It is also worth noting that only half of the solution must be determined.



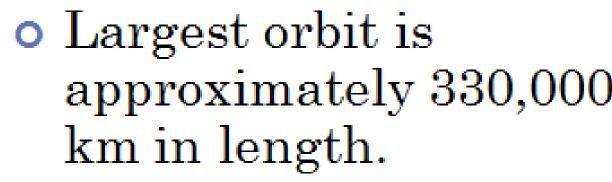


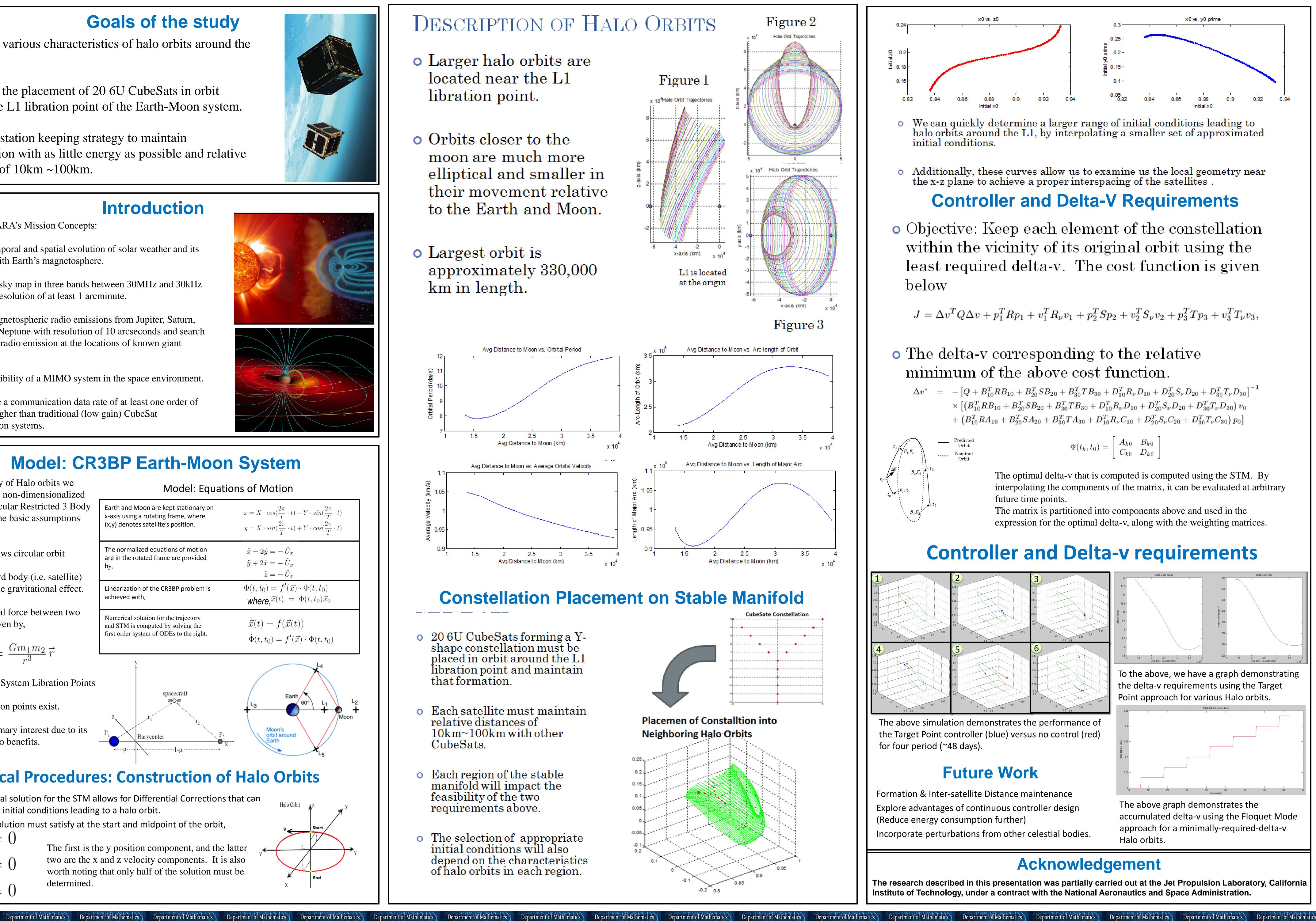






- Larger halo orbits are located near the L1 libration point.
- Orbits closer to the moon are much more to the Earth and Moon.





- 20 6U CubeSats forming a Y-
- Each satellite must maintain
- Each region of the stable
- The selection of appropriate initial conditions will also

